

Fluid Phase Equilibria of Binary *n*-Alkane + Squalane Systems

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In this study, the phase behavior of binary systems of squalane (C₃₀H₆₂, 2,6,10,15,19,23-hexamethyltetracosane) with ethane, and propane, is investigated. For both systems, vapor–liquid equilibrium data were measured using the synthetic method in the temperature range (263 to 473) K and pressure range (0.2 to 16) MPa. Also a liquid–liquid–vapor curve was determined for the ethane + squalane system. The experiments were carried out for various mixtures covering almost the whole composition range. Additionally, the experimental data have been modeled using the Soave–Redlich–Kwong equation of state using two adjustable parameters in the classical mixing rules.

Introduction

Phase behavior measurements for binary systems of short and long paraffins are very important both for practical process design and for developing theoretical models. For example, these systems can be considered as models for mixtures of oligomers and polymers in low-molar-mass solvents that are of interest for the design of dewaxers in a polymer plant. Such data can also be used to obtain the parameters for different types of thermodynamic models such as equations of state, group contribution methods and molecular simulation calculations, models that can be used in further predictions.

Although systems of short and long chain normal alkanes have been extensively studied, very little information has been published for systems with branched long-chain alkanes. Paas et al.¹ have reported some work on binary systems of squalane with methane and ethane. However, their work focused only on mixtures with high concentration of ethane (more than 0.9 in mole fraction) and low and very low temperatures. Recently, Aalto et al.² have reported some bubble point pressures and densities for the binary propane + squalane in the vicinity of the critical point of propane. In this paper, we present fluid phase equilibrium data for the two binary systems, ethane + squalane and propane + squalane, over wide ranges of temperature, composition, and pressure.

Experimental Section

Method. The experiments were carried out using the so-called Cailletet apparatus according to the synthetic method. In a binary mixture with constant overall composition, a two-phase equilibrium is bivariant; therefore, by setting the temperature to a certain constant value, only the pressure could be varied until a phase change is observed visually. Bubble- and dew- points are the points at which the last bubble of vapor, or the last droplet of liquid, disappears, respectively ($L + V \rightarrow L$ or $L + V \rightarrow V$). The bubble- and dew-point pressures are measured visually as

a function of temperature for mixtures with known composition.

A three-phase equilibrium is monovariant in a binary mixture with a given composition, so if the temperature is fixed, the volume can be adjusted to observe three phases and the recorded pressure is the equilibrium pressure.

A detailed description of the apparatus and the procedure is given elsewhere.³ A sample of the mixture with known composition is confined in a narrow glass tube, mounted in a thermostatic bath. During the experiments, the temperature is maintained constant to within 0.03 K. The temperature is measured with a Pt100 resistance thermometer, which was calibrated against a standard thermometer with an accuracy of ± 0.01 K. The uncertainty in the measured temperature was approximately 0.02 K. The pressure is applied hydraulically and is measured with a dead weight pressure gauge (Budenberg) with an accuracy of 0.005 MPa. The experiments were done for various mixtures covering almost the whole composition range in a temperature range of (263 to 473) K and a pressure range of (0.2 to 16) MPa.

Materials. The mole fraction purity of the ethane (Messer Griesheim) and the propane (Messer Griesheim) used was greater than 0.9995. The squalane was purchased from Merk Schuchardt as "squalane for synthesis" with a minimum purity of at least 99% (GC) and was used without further purification.

Results. The measured p - T equilibrium data for the binary system ethane + squalane at 12 different compositions are summarized in Table 1. It has been found that this binary exhibits partial miscibility in the liquid phase; that is, in this binary, a three-phase equilibrium liquid–liquid–vapor with lower (LCEP) and upper (UCEP) critical endpoints exists. In the LCEP, the heavy liquid and the light liquid become critical in the presence of a noncritical vapor phase ($L_2 = L_1 + V$). In the UCEP, the light liquid and the vapor become critical in the presence of a noncritical heavy liquid phase ($L_2 + L_1 = V$). The liquid–liquid split occurs in mixtures with composition rich in ethane. For such compositions the transitions from the two-phase $L_1 + V$ to the homogeneous region L_1 , and from the two-phase region $L_1 + L_2$ to the homogeneous region L_1 , and liquid–liquid–vapor (L_1L_2V) equilibrium data were mea-

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Table 1. Experimental Vapor–Liquid and Liquid–Liquid Equilibrium Data for the System [x Ethane + (1 - x) Squalane] at Fixed Molar Composition

x		T/K	p/MPa	T/K	p/MPa	T/K	p/MPa	x		T/K	p/MPa	T/K	p/MPa	T/K	p/MPa
0.9799	L ₁ + V → L ₁	248.78	1.265	263.57	1.885	273.59	2.405	0.7012	L + V → L	442.79	10.950	452.81	11.425	462.81	11.875
		283.57	3.035	293.60	3.790	472.79	12.290								
	L ₁ + L ₂ → L ₁	297.54	4.380	298.79	4.665	300.50	5.040		0.5975	L + V → L	263.78	0.885	273.62	1.195	283.59
303.56	5.705	313.57	7.765	323.56	9.660	293.51	1.735	303.50			2.050	313.58	2.400		
328.61	10.566					322.98	2.825	323.61			2.770	332.79	3.145		
0.9752	L ₁ + V → L ₁	263.53	1.885	273.52	2.405	283.46	3.030	0.5031	L + V → L	273.52	0.865	283.69	1.070	293.52	1.265
		293.55	3.785	294.44	3.860					303.50	1.495	313.57	1.745	323.03	1.990
	L ₁ + L ₂ → L ₁	297.40	4.380	298.46	4.620	299.37	4.820			332.98	2.270	342.90	2.570	352.77	2.855
	300.34	5.035	301.35	5.260	302.38	5.485	362.36			3.165	372.43	3.480	382.68	3.780	
	303.43	5.715	303.46	5.720	304.42	5.925	392.25			4.100	402.38	4.405	412.46	4.705	
	305.32	6.120	306.30	6.280	307.07	6.490	422.71			4.995	432.51	5.290	442.71	5.560	
0.9504	L ₁ + V → L ₁	263.59	1.865	273.58	2.385	283.52	3.015	0.3989	L + V → L	273.64	0.610	283.53	0.745	293.59	0.895
		293.57	3.785							303.53	1.050	313.60	1.225	323.48	1.405
	L ₁ + L ₂ → L ₁	298.48	4.410	303.43	5.515	308.48	6.600			332.67	1.580	333.66	1.600	342.60	1.775
	313.41	7.615	318.40	8.605	323.41	9.560	352.73			1.990	362.89	2.195	372.89	2.410	
	332.57	11.225	342.50	12.865	352.47	14.365	382.84			2.615	392.74	2.835	402.71	3.035	
0.8992	L + V → L	263.49	1.815	273.58	2.320	283.49	2.925	412.63	3.240	422.64	3.440	432.65	3.640		
		293.52	3.665	303.49	4.575	313.49	5.870	442.52	3.830	452.66	4.015	462.66	4.190		
		323.05	7.520	333.06	9.235	343.03	10.850	472.68	4.360						
		353.00	12.360	362.94	13.760	372.89	15.050								
0.8498	L + V → L	263.55	1.655	273.59	2.115	283.69	2.665	0.2994	L + V → L	273.57	0.430	283.58	0.530	293.68	0.630
		293.48	3.300	303.51	4.065	313.55	4.965			303.50	0.720	313.48	0.830	323.62	0.955
		323.50	6.015	332.92	7.230	342.92	8.525			332.92	1.075	333.66	1.080	342.75	1.200
		353.00	9.825	363.03	11.085	373.03	12.280			352.72	1.330	362.79	1.470	372.75	1.605
0.8007	L + V → L	263.45	1.500	273.42	1.900	283.49	2.380	382.70	1.745	392.82	1.890	402.76	2.025		
		293.46	2.935	303.51	3.580	313.49	4.300	412.35	2.160	422.39	2.295	432.49	2.425		
		323.45	5.110	332.95	5.945	342.82	6.885	442.52	2.560	452.57	2.685	462.59	2.805		
		352.79	7.860	362.87	8.860	372.91	9.850	472.60	2.925						
		382.87	10.790	392.80	11.695	402.79	12.550								
0.7012	L + V → L	412.83	13.365	422.85	14.120	432.86	14.825	0.2046	L + V → L	283.60	0.330	293.53	0.385	303.60	0.450
		263.48	1.205	273.39	1.505	283.48	1.870			313.56	0.520	323.48	0.600	332.99	0.670
		293.59	2.270	299.35	2.540	313.46	3.210			342.92	0.745	352.87	0.825	362.85	0.915
		323.45	3.750	332.97	4.300	342.94	4.905			372.79	1.000	382.75	1.090	392.77	1.170
		352.85	5.525	362.83	6.165	372.56	6.805			402.82	1.260	412.52	1.345	422.85	1.425
		382.78	7.460	392.76	8.095	402.72	8.715			422.85	1.425	432.82	1.520	442.84	1.600
412.76	9.315	422.77	9.850	432.79	10.435	452.91	1.655	462.75	1.740	472.76	1.815				

Table 2. Experimental Data of the Three-Phase Equilibrium L₁L₂V in the Ethane–Squalane System

T/K	p/MPa	T/K	p/MPa	T/K	p/MPa
295.57	3.930 ^a	298.79	4.231	302.53	4.581
295.71	3.961	299.33	4.287	303.43	4.685
296.00	3.979	300.34	4.374	304.42	4.775
296.53	4.028	300.94	4.436	305.32	4.865
297.38	4.105	301.35	4.474	306.51	4.996
297.89	4.166	302.37	4.570	306.69	5.013 ^b
298.30	4.196				

^a LCEP (L₂ = L₁ + V). ^b UCEP (L₂ + L₁ = V).

sured (see Figure 1). As depicted in Figure 1, which present an isopleth for $x_{\text{ethane}} = 0.9504$, the intersection of the L₁ + V → L₁ and L₂ + L₁ → L₁ curves gives a point on the three-phase equilibrium line. The three-phase equilibrium data and both the critical end points are presented in Table 2. The two critical end points measured in this work are slightly different from the ones reported by Paas et al.,¹ i.e., $T_{\text{LCEP}} = 295.7$ K, $p_{\text{LCEP}} = 3.87$ MPa, and $T_{\text{UCEP}} = 306.8$ K, $p_{\text{UCEP}} = 4.92$ MPa. In accordance with ref 1, an additional liquid–liquid immiscibility should occur in this system at very low temperatures. However, this could not be measured with the experimental setup used in this work and can be observed only in strongly undercooled liquid mixtures. Therefore, the present work suggests that the fluid phase behavior of this system most likely belongs to type V in the classification of Van Konynenburg and Scott.⁴

In the system propane + squalane, no liquid–liquid immiscibility is found in the range of temperature and pressure covered by this work. The measured bubble-point

(L + V → L), dew-point (L + V → V), and critical-point (L = V) temperatures and pressures for this binary, at 13 different compositions, are given in Table 3. Therefore, according to the present, work the fluid phase behavior in

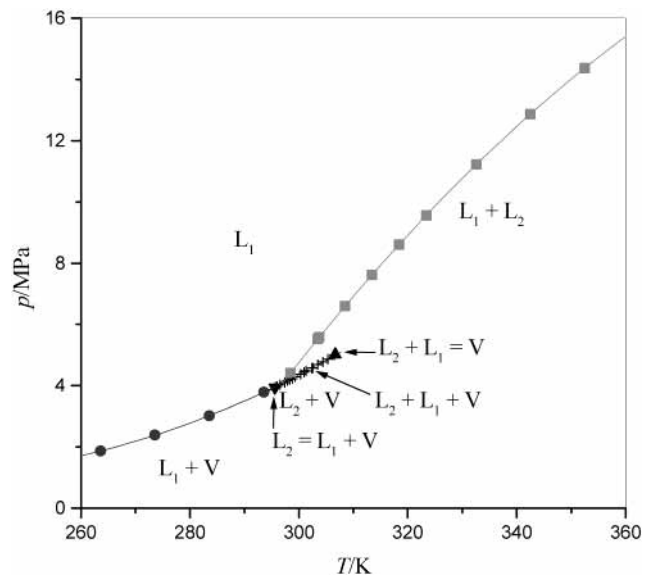


Figure 1. p - T diagram showing two-phase transition curves and the three-phase equilibrium line for the binary system [x ethane + (1 - x) squalane] with $x = 0.9504$: ●, L₁ + V → L₁; ■, L₂ + L₁ → L₁; +, L₂ + L₁ + V; ▼, LCEP (L₂ = L₁ + V); ▲, UCEP (L₂ + L₁ = V).

Table 3. Experimental Vapor–Liquid Equilibrium Data for the System [x Propane + (1 - x) Squalane] at Fixed Molar Composition

<i>x</i>	<i>T</i> /K	<i>p</i> /MPa	<i>T</i> /K	<i>p</i> /MPa	<i>T</i> /K	<i>p</i> /MPa	<i>x</i>	<i>T</i> /K	<i>p</i> /MPa	<i>T</i> /K	<i>p</i> /MPa	<i>T</i> /K	<i>p</i> /MPa		
0.9803	L + V → L	263.49	0.349	273.49	0.476	283.46	0.635	0.9000	L + V → L	373.45	3.979	383.42	4.689	393.33	5.479
		293.45	0.831	303.40	1.069	313.41	1.354			403.39	6.336	403.28	6.342	413.11	7.212
		323.40	1.690	333.43	2.084	343.42	2.540			422.66	8.052	432.79	8.887	442.59	9.652
		353.36	3.062	363.35	3.669	373.35	4.374			452.20	10.357	461.96	11.012	471.86	11.607
		383.36	5.227							263.44	0.274	273.47	0.372	283.44	0.494
	L = V	393.46	6.123						293.44	0.644	303.40	0.823	313.38	1.037	
		394.39	6.303	395.41	6.403	403.39	7.163		323.39	1.286	333.32	1.570	343.27	1.893	
	0.9751	L + V → L	413.40	8.063	423.41	8.888	433.48		9.638	353.23	2.260	363.22	2.669	373.21	3.121
			263.56	0.347	273.62	0.474	283.59		0.634	383.21	3.614	393.22	4.148	403.24	4.713
			293.56	0.832	303.50	1.069	303.56		1.071	413.25	5.299	423.26	5.908	433.42	6.519
313.50			1.357	322.97	1.680	323.58	1.697	443.41	7.119	453.39	7.704	463.34	8.269		
332.93			2.075	342.85	2.525	352.74	3.040	473.34	8.809						
L = V		362.76	3.655	367.78	4.000	372.78	4.360	263.48	0.225	273.52	0.305	283.45	0.403		
		382.70	5.200	387.68	5.685	392.66	6.170	293.47	0.524	303.42	0.667	313.40	0.833		
0.9701		L + V → L	397.66	6.660					323.41	1.025	333.41	1.246	343.29	1.492	
			398.67	6.755					353.28	1.766	363.27	2.069	373.27	2.399	
			399.16	6.805	400.70	6.945	402.65	7.140	383.25	2.752	393.23	3.134	403.23	3.526	
	407.65		7.600	412.68	8.045	422.66	8.885	413.25	3.937	423.22	4.360	433.18	4.788		
	432.65		9.650	442.65	10.335	452.68	10.940	443.28	5.219	453.22	5.648	463.22	6.069		
	L = V	462.68	11.460	472.73	11.905			473.28	6.480						
		263.46	0.333	273.50	0.459	283.47	0.617	263.47	0.180	273.49	0.242	283.46	0.320		
	0.9600	L + V → L	293.45	0.814	303.39	1.047	313.38	1.327	293.48	0.416	303.40	0.530	313.39	0.656	
			323.35	1.656	333.33	2.044	343.35	2.512	323.37	0.802	333.36	0.961	343.34	1.152	
			353.35	3.032	363.36	3.636	373.51	4.349	353.29	1.357	363.28	1.581	373.26	1.824	
383.42			5.192	393.48	6.176	403.48	7.141	383.29	2.084	393.26	2.354	403.27	2.637		
404.45			7.236					413.30	2.932	423.28	3.234	433.30	3.541		
L = V		406.44	7.416					443.30	3.852	453.29	4.154	463.28	4.462		
		408.46	7.601	413.48	8.051	423.45	8.891	473.28	4.763						
0.9499		L + V → L	428.48	9.291	433.61	9.672	443.51	10.357	298.89	0.360	303.81	0.407	313.44	0.499	
			453.51	10.977	463.52	11.512	473.51	11.967	323.39	0.609	333.30	0.738	343.31	0.872	
			263.45	0.340	273.41	0.464	283.44	0.621	353.50	1.024	363.50	1.186	373.49	1.360	
	293.42		0.813	303.40	1.047	313.38	1.327	383.49	1.549	393.52	1.741	403.53	1.947		
	323.35		1.655	333.35	2.040	343.30	2.489	413.56	2.157	423.63	2.372	433.68	2.598		
	L = V	353.23	3.003	363.20	3.599	373.17	4.296	443.36	2.807	453.32	3.032	463.27	3.249		
		383.19	5.134	393.39	6.142	403.34	7.137	297.92	0.259	304.56	0.300	313.42	0.362		
	0.9200	L + V → L	413.34	8.072	423.31	8.937	428.31	9.342	323.35	0.440	333.30	0.529	343.27	0.624	
			430.30	9.497	432.29	9.647	438.27	10.092	353.24	0.731	363.35	0.846	373.31	0.967	
			442.30	10.372					383.28	1.097	393.26	1.231	403.25	1.373	
442.77			10.407					413.22	1.528	423.20	1.665	433.16	1.814		
443.30			10.437	448.30	10.772			443.14	1.970	453.08	2.119	463.07	2.272		
L = V		263.43	0.338	273.48	0.463	283.46	0.618	473.06	2.426						
		293.44	0.809	303.44	1.042	313.42	1.320	315.97	0.273	325.31	0.325	332.42	0.366		
0.9000		L + V → L	323.41	1.651	333.41	2.041	343.46	2.502	341.83	0.427	347.72	0.467	352.71	0.503	
			353.33	3.016	363.29	3.612	373.20	4.304	362.61	0.581	372.72	0.666	382.71	0.753	
			373.20	4.304	383.14	5.130	393.08	6.092	392.69	0.844	402.67	0.939	412.58	1.038	
	402.94		7.082	412.70	8.017	422.58	8.882	422.66	1.140	432.68	1.241	442.65	1.344		
	432.30		9.662	442.13	10.382	447.18	10.723	452.68	1.449	462.66	1.554	473.82	1.669		
	L = V	447.21	10.717	452.16	11.038	457.12	11.333	332.87	0.182	342.79	0.205	352.77	0.237		
		461.09	11.558					362.74	0.271	372.76	0.307	382.71	0.346		
	L + V → L	273.52	0.441	283.50	0.587	293.43	0.765	392.72	0.388	402.71	0.430	412.70	0.474		
		303.40	0.987	263.49	0.323	313.42	1.245	422.70	0.519	432.73	0.565	442.72	0.610		
		323.40	1.558	333.41	1.912	333.53	1.918	453.22	0.658	463.21	0.705	473.39	0.751		
343.52		2.330	353.51	2.808	363.47	3.358									

the system propane + squalane is of type I in the before mentioned classification,⁴ even though at lower temperatures a liquid–liquid immiscibility with an upper critical solution temperature as for a type II behavior might occur.

Isothermal *p, x* sections were obtained by interpolation from polynomials fitted to the *p, T* data.

Modeling

The bubble-point VLE data of both binary systems were modeled with the Soave–Redlich–Kwong (SRK) equation of state⁵ using the VLE95 program⁶ for fluid phase equilibrium calculations. The classical one-fluid van der Waals mixing rules were applied as follows:

$$a = \sum_{i=1}^2 \sum_{j=1}^2 x_i x_j (a_i a_j)^{0.5} (1 - k_{ij}) \quad (1)$$

$$b = \sum_{i=1}^2 \sum_{j=1}^2 x_i x_j \frac{(b_i + b_j)}{2} (1 - l_{ij}) \quad (2)$$

Figures 2 and 3 show that the calculated VLE curves in the two investigated systems are in agreement with the experimental isothermal *p, x* data. The optimized values of the interaction parameters, *k_{ij}* and *l_{ij}*, for each isotherm, and the average absolute deviation in estimating the saturation pressures, AADP, eq 3 are summarized in Table 4.

$$\text{AADP} = \frac{1}{\text{NEXP}} \sum_{i=1}^{\text{NEXP}} \left| \frac{p_i^{\text{exp}} - p_i^{\text{calc}}}{p_i^{\text{exp}}} \right| 100 \quad (3)$$

The prediction of three-phase region for the binary mixture ethane + squalane was performed with the binary interaction parameters set to zero and with the binary interaction parameters fitted to vapor–liquid equilibrium data at the temperature of LCEP. The calculated critical curve and the predicted the three-phase curve are shown in Figures 4 and 5. The results obtained are in qualitative agreement with the experimental data.

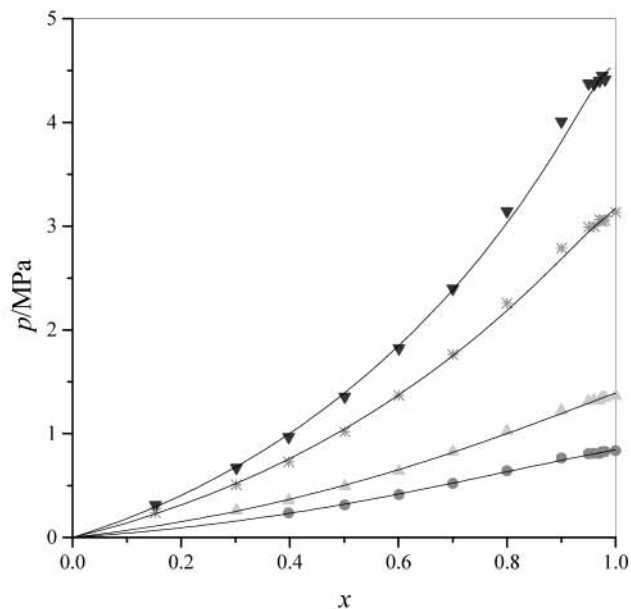


Figure 2. Vapor-liquid equilibria for [x propane + (1 - x) squalane] depicted as isothermal p , x sections. Experimental data: ●, 293.15 K; ▲, 313.15 K; *, 353.15 K; ▼, 373.15 K; solid lines, calculated with SRK-EoS and k_{ij} and l_{ij} from Table 4.

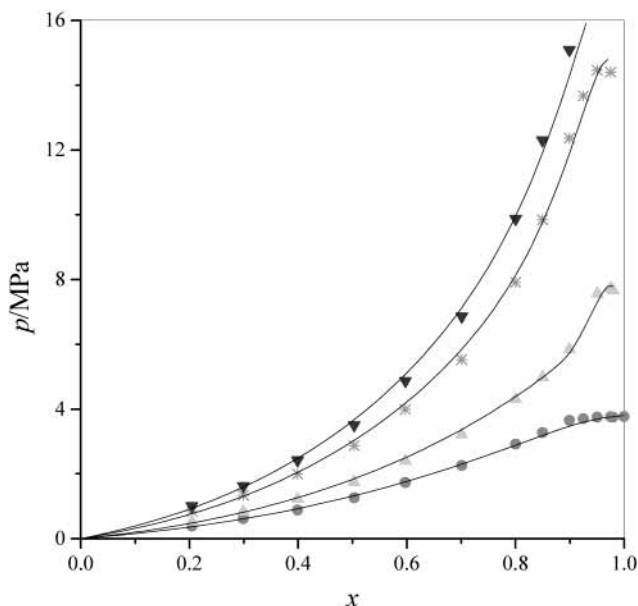


Figure 3. Vapor-liquid equilibria for [x ethane + (1 - x) squalane] depicted as isothermal p , x sections. Experimental data: ●, 293.15 K; ▲, 313.15 K; *, 353.15 K; ▼, 373.15 K; solid lines, calculated with SRK-EoS and k_{ij} and l_{ij} from Table 4.

Table 4. Modeling Results of the Vapor - Liquid Equilibria

T/K	ethane-squalane system			propane-squalane system		
	k_{ij}	l_{ij}	AADP %	k_{ij}	l_{ij}	AADP %
293.15	0.0151	0.0229	2.38	0.0014	0.0214	1.38
313.15	0.0236	0.0289	3.18	-0.0059	0.0189	1.65
353.15	0.0239	0.0350	3.52	-0.0090	0.0203	1.93
373.15	0.0209	0.0364	3.68	-0.0080	0.0235	2.20

Discussions and Conclusions

This paper presents fluid phase equilibrium data for the binary systems ethane + squalane and propane + squalane. The results confirm the occurrence of a liquid-liquid-vapor equilibrium in the ethane + squalane system at temper-

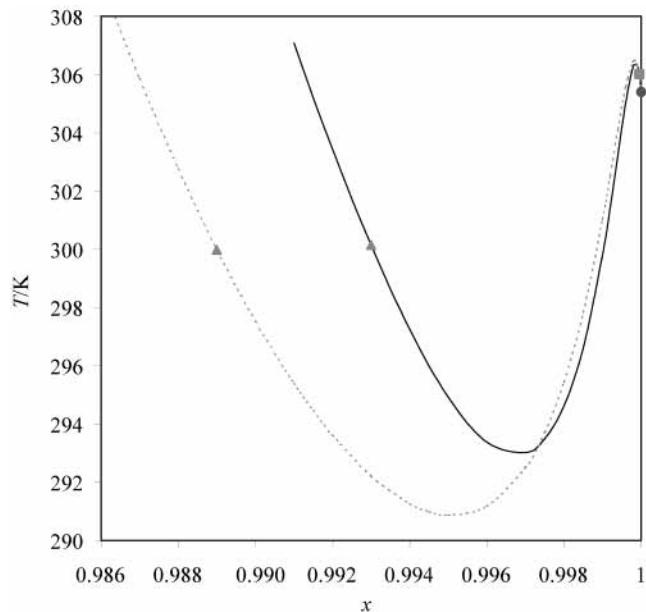


Figure 4. T - x projection of the critical curve for the system [x ethane + (1 - x) squalane]. Solid line, calculated with SRK-EoS and $k_{ij} = l_{ij} = 0$; dashed line, calculated with SRK-EoS and k_{ij} and l_{ij} from VLE at LCEP; ●, ethane CP; ■, UCEP; ▲, LCEP.

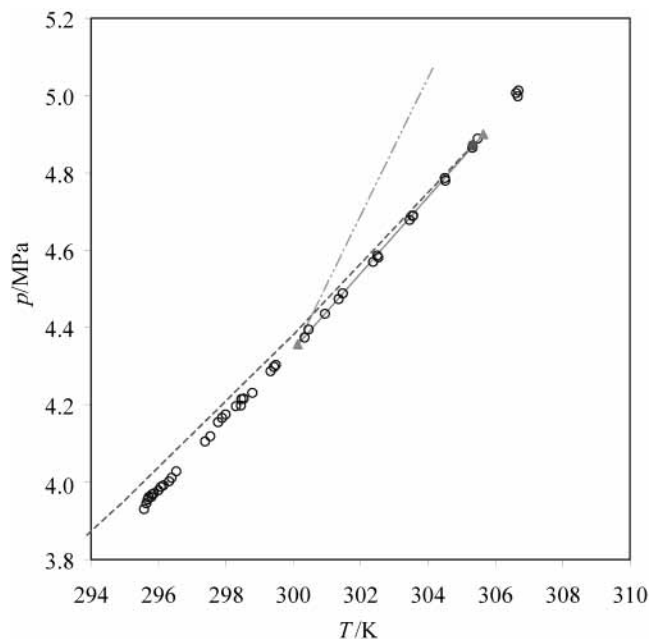


Figure 5. p - T projection of the three phase curve and of the critical line for the system ethane + squalane: ○, LLVE experimental data; ---, ethane LVE; ●, ethane CP; -▲-, LLVE calculated with SRK-EoS and $k_{ij} = l_{ij} = 0$; - · - · -, critical line ($L_1 = L_2$) calculated with SRK-EoS and $k_{ij} = l_{ij} = 0$.

atures close to the critical point of ethane. The present measurements indicate that this binary is of type V in the classification of Van Konynenburg and Scott.⁴ In the temperature range covered in this work, the system propane + squalane behaves as a type I system in the before mentioned classification. However, according to some earlier work¹ the systems ethane + squalane and propane + squalane should exhibit type IV and type II behavior, respectively. Further investigations in strongly undercooled conditions should be done to confirm this hypothesis (i.e., to show the occurrence of a liquid-liquid demixing at low temperatures with an upper critical

solution temperature). The VLE modeling results and the predicted LLV line are in qualitative agreement with the experimental data.

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